

DETERMINING HOW EFFECTIVE A TREATMENT WILL BE FOR AN INDIVIDUAL PATIENT

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Background

- MacArthur Network and what followed (Skimming the top).
- Theme: The value of clinical research is measured by the degree to which it improves the impact of clinical decision-making on individual patients.
- A study that well addresses that problem is likely to be more powerful, more cost-effective, and to have a greater impact on patient care.
- Insanity: doing the same thing over and over again and expecting different results. (Albert Einstein).

Effect Sizes - I

- Meehl: All null hypotheses (of randomness) are false. True?
 - Large enough samples sizes and enough RCTs will eventually result in one or two or more $p < .05$ s.
- The p-value indicates the adequacy of the design (sample size, measurement) to detect the deviation from randomness, not the clinical importance of the treatment choice.

Effect Sizes - II

- An appropriately chosen effect size: a population parameter (estimated in a sample) that indicates the clinical importance of the finding.
 - In each RCT report effect size and its confidence interval (CONSORT, APA)
 - When multiple RCTs done, meta analysis using that effect size will give a more precise estimator of the population parameter. `

Which Effect Size to compare T1 vs T2 in a RCT?

- Cohen's d: To compare normal distributions with equal variances, yes.
- Odds Ratio: Never!
- $AUC = \text{Prob}(T1 > T2) + .5 \text{Prob}(T1 = T2)$
 - AUC estimated by $U/(mn)$, where m and n are the sample sizes.
 - Where d appropriate $AUC = \Phi(d/\sqrt{2})$.
- $SRD = \text{Prob}(T1 > T2) - \text{Prob}(T1 < T2) = 2AUC - 1$.
 - For success/failure outcome, SRD=Success Rate Difference.
- $NNT = \text{Number Needed to Treat} = 1/SRD$.

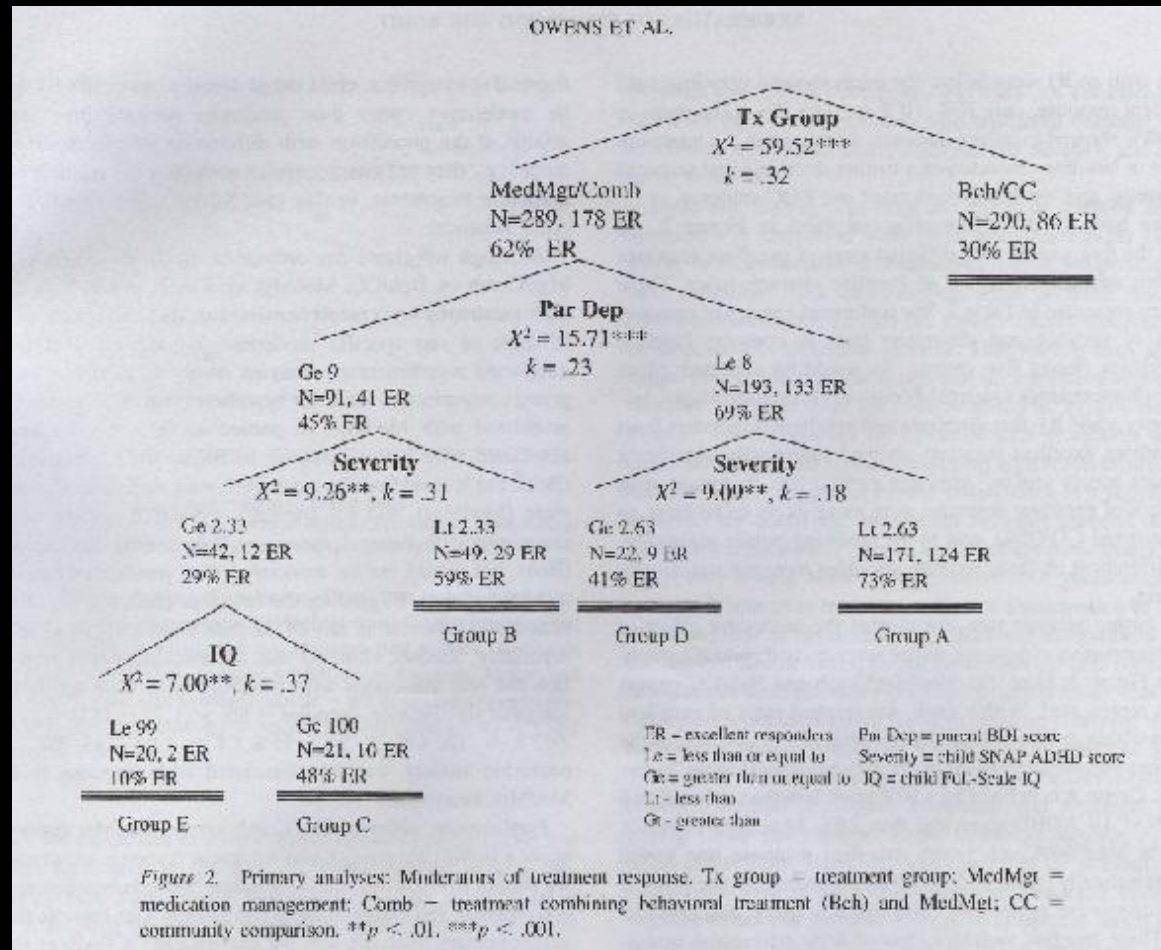
Definition of Moderators of Treatment - I

- The overall effect size comparing T1 and T2 in a RCT indicates the AVERAGE effect size over the patients in the population, NOT the effect on any individual patient.
- M is a moderator of treatment choice (T: T1 versus T2) on the outcome (O) *if* the effect size of T on O changes depending on what M is.
 - Personalized Medicine.

Definition of Moderators of Treatment - II

- MacArthur Model criteria for Moderators:
 - Temporal Precedence: M precedes T precedes O in time.
 - Correlation: M and T uncorrelated.
 - Effect Size: The effect size of T on O changes depending on what M is.
- In a RCT, any baseline (pre-randomization) variable satisfies the first two criteria.

Example: MTA search



Messages - I

- For any T1 vs T2 comparison, there are many baseline factors, but only a few moderators of treatment on outcome: Need for exploration (hypothesis-generation) to detect moderators.
- The result of exploration is rationale and justification for **hypotheses** to be tested in future RCTs (and the information needed to design powerful such studies). It is not **conclusions**.

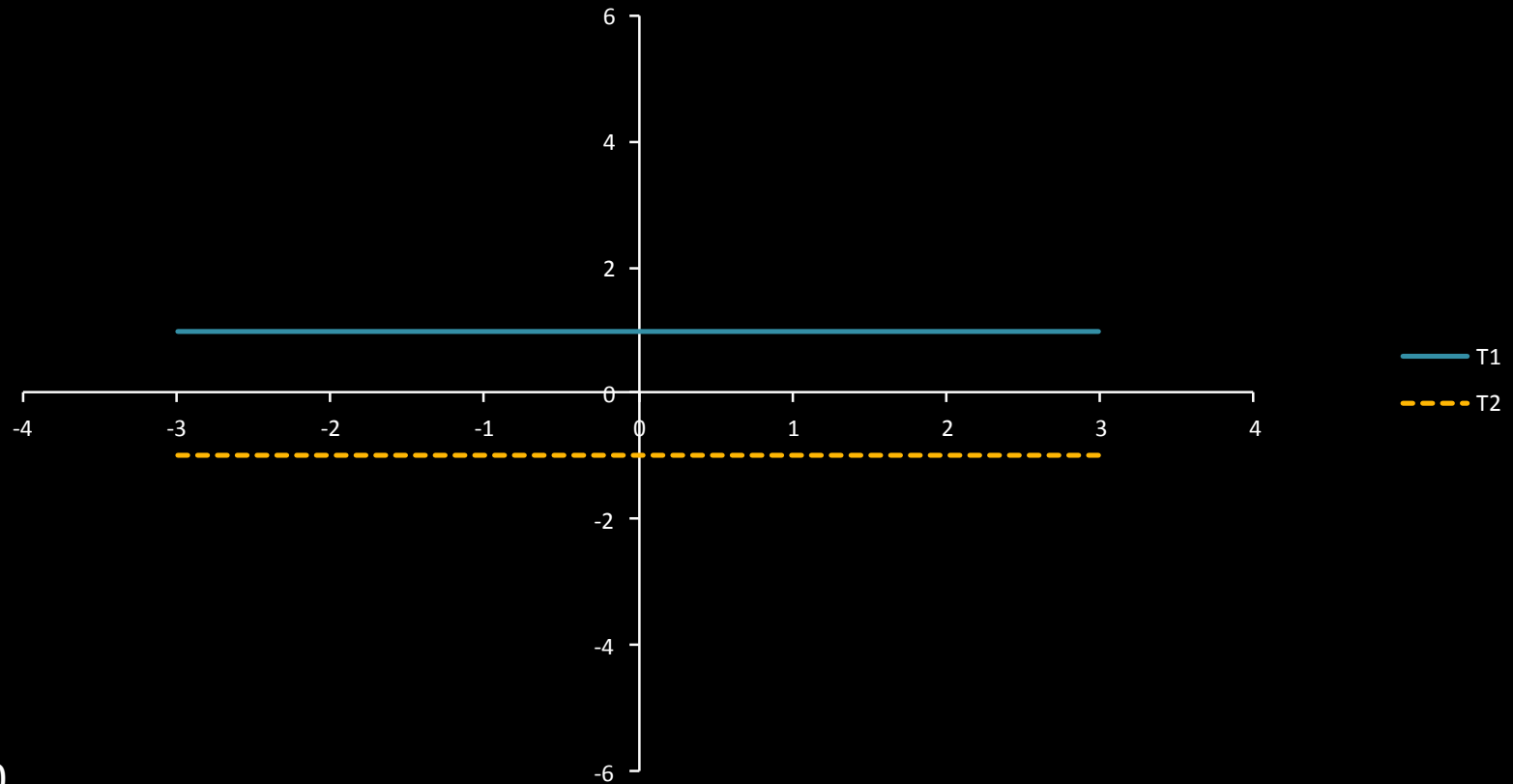
Messages - II

- What you expect will moderate, may not. Surprise!
- A single moderator may not much improve clinical decision-making; decision rules based on **multiple moderators** will likely do much better, and will bring medical decision-making closer to the goals of Personalized Medicine.

How to search for a moderator— Linear Model

- Linear Model: $O = b_0 + b_1T + b_2M + b_3TM + e$
- Centering: T coded +1/2 and -1/2; M standardized to a mean of 0 and variance 1.

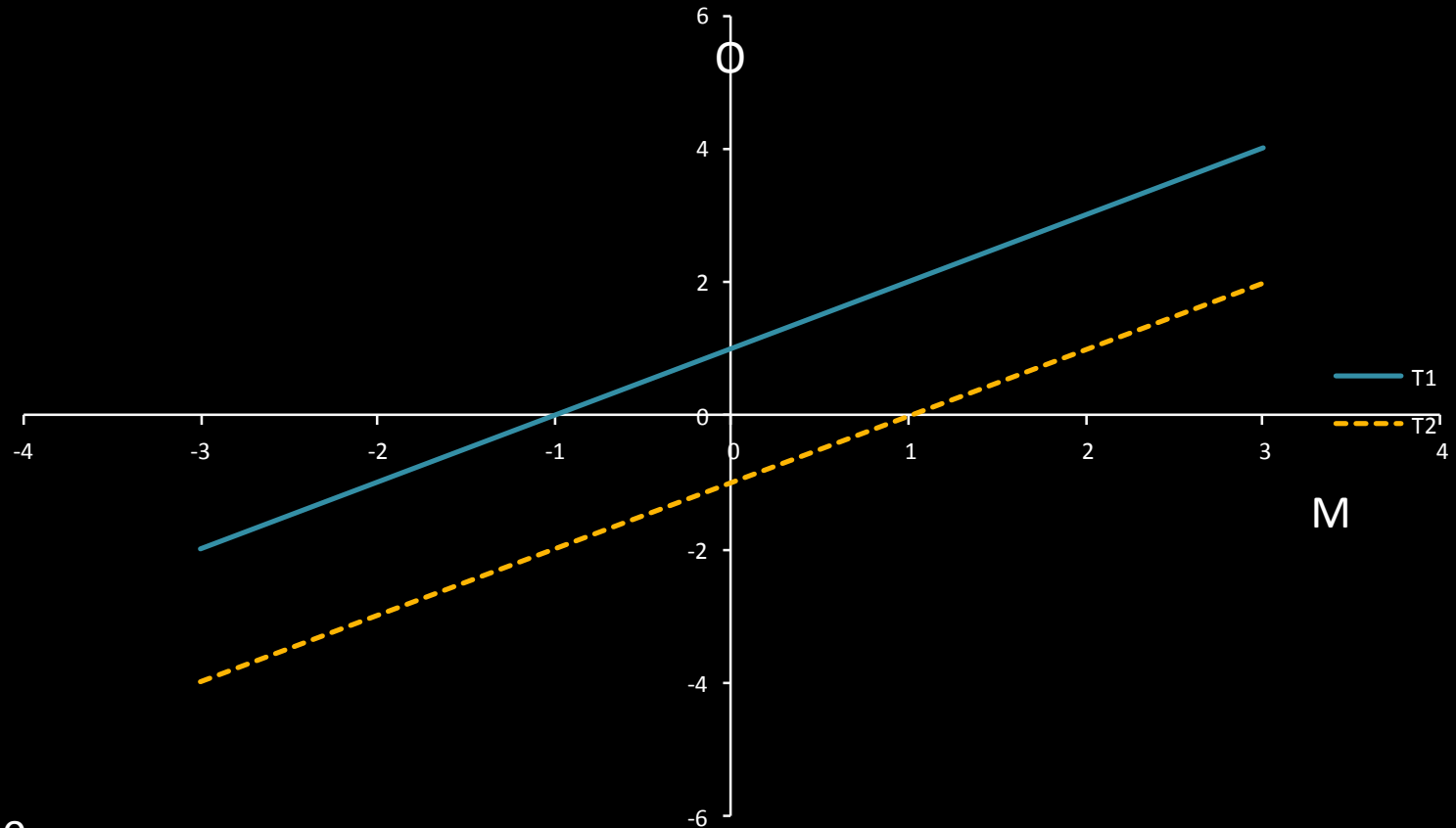
Factor is irrelevant to treatment



$$b_2 = b_3 = 0$$

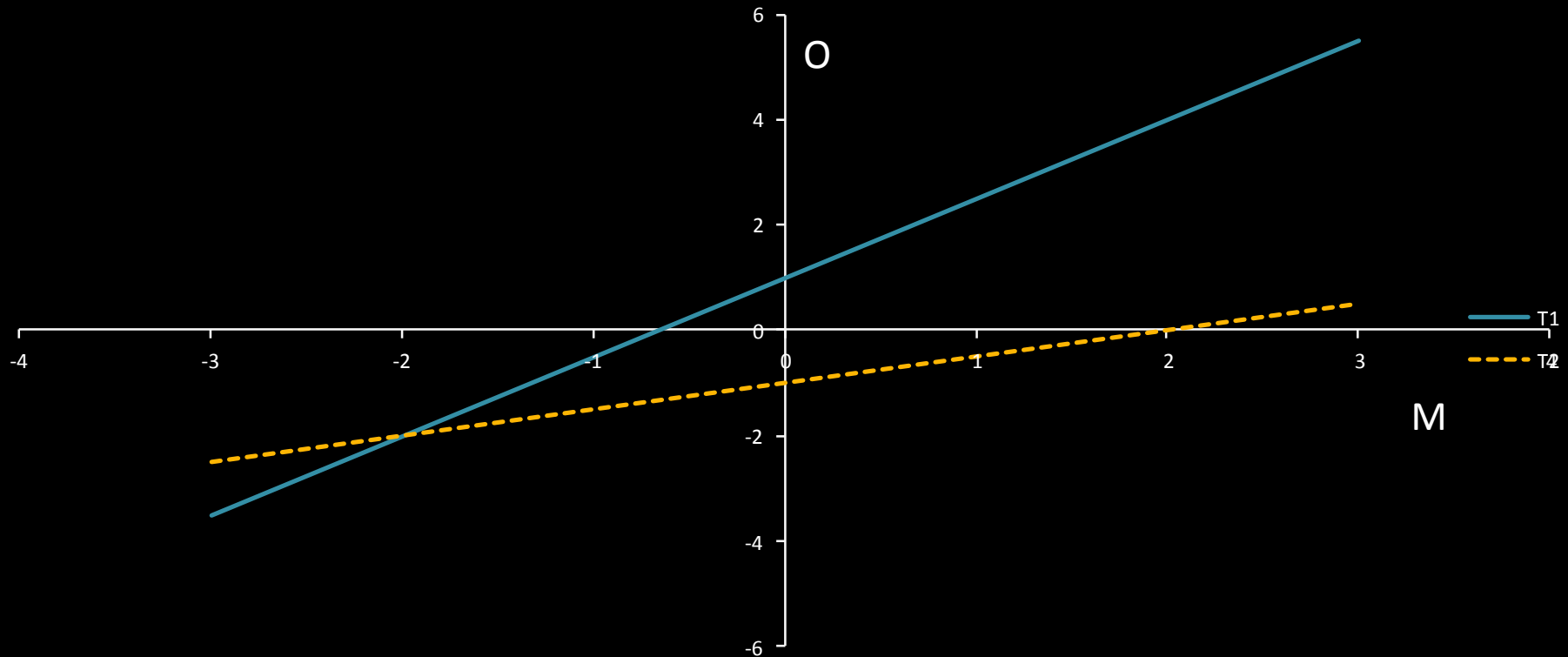
$$d_1 = b_1 / \sigma_e = \text{Overall ES} = \text{ES}(\text{each M})$$

Factor is A non-specific predictor



Here $b_3=0$, $b_2 \neq 0$
 $d_1 = b_1 / \sigma_e = ES(\text{each } M)$

Factor is a Moderator



Here $b_3 \neq 0$.

If $T1 > T2$ for all M, or $T1 < T2$ for all M, then M is a “quantitative moderator”.

If $T1 > T2$ for some M and $T1 < T2$ for others, then M is a “qualitative moderator”.

$$d_1 = b_1 / \sigma_e = ES(M=0)$$

Moderator Effect Size - I

- We need a Moderator Effect size:
 - To compare and convey the potential impact of different moderators.
- b_3 ??? Not invariant under linear transformation of O.
- $d_3 = b_3 / \sigma_e$??? Ignores the relative contributions of M and T separately.

Moderator Effect Size - II

- The treatment effect size T1 versus T2=Overall ES:
Overall ES= $d_1/\sqrt{(d_2^2+d_3^2/4+1)}$.
 - d_1 is the Cohen's d for subjects with $M=0$.
 - Attenuation of the magnitude of ES_1 due to d_2 and/or d_3 .
- $NspES=d_2/\sqrt{(d_2^2+d_3^2/4+1)}$.
- $ModES=(d_3/2) / \sqrt{(d_2^2+d_3^2/4+1)}$.
- Then Overall ES= $d_1(1-NspES^2-Mod ES^2)$.

MODERATOR EFFECT SIZE - III

- Randomly select one patient from T1 and one from T2, compute ΔO , the difference in outcome, ΔM , the difference in their Ms, and AM the average of their Ms.
- Then $\Delta O = b_1 + b_2 \Delta M + b_3 AM + \Delta e$.
 - But ΔM and AM are uncorrelated, since the two Ms have equal variances (Pitman).
- Thus:
 - Correlation $(\Delta O, AM) = \text{ModES}$.
 - Correlation $(\Delta O, \Delta M) = \text{NspES}$.

An Optimal moderator - I

- Have possible moderators M_1, M_2, M_3, \dots
 - Remove any that don't make sense, that are badly measured.
 - Remove redundancies.
- For each M , test, and estimate the Mod ES and its confidence interval (bootstrap).
 - Compare the Mod ES of the moderators.

An Optimal moderator - II

- Use a multiple regression model with ΔO from all possible randomly paired subjects, with independent measures AM_1, AM_2, \dots as the predictors. This produces weights w_1, w_2, \dots
- The optimal moderator is $M^* = \sum w_j M_j$.
 - Get its Mod ES and the confidence interval
- Get independent verification!

Conclusion

- Importance of clinically meaningful effect sizes (and their confidence intervals)
- Importance of moderators in RCTs and in clinical decision-making.
- Exploration to:
 - Identify individual moderators and their effect sizes.
 - Identify an optimal moderator and its effect size.
- Independent Validation
- Treatment decision algorithms for clinical use (apps?).
- Changing the direction of subsequent clinical research by focusing separately on moderated subgroups.

Transition

- Everything depends on having an outcome measure (O) that is reliable, valid, and that is sensitive to crucial individual differences in treatment response among the patients (harms and benefits).
- Ellen....